

# Singularity Functions To Enhance Monitoring In The Last Planner System



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# Presentation Outline

Research Gap / Goal

Last Planner System

Control in Planning

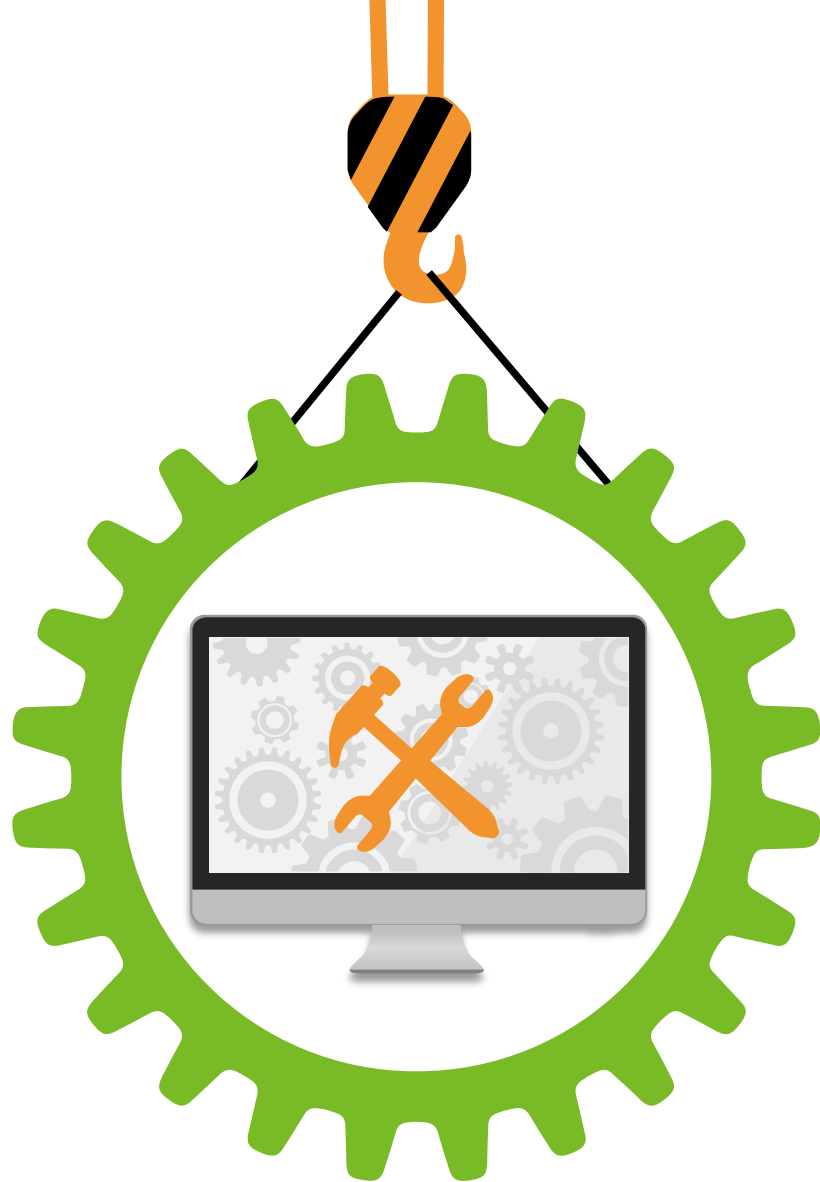
Singularity Functions

Methodology

Developed Tool

Simulation

Conclusion

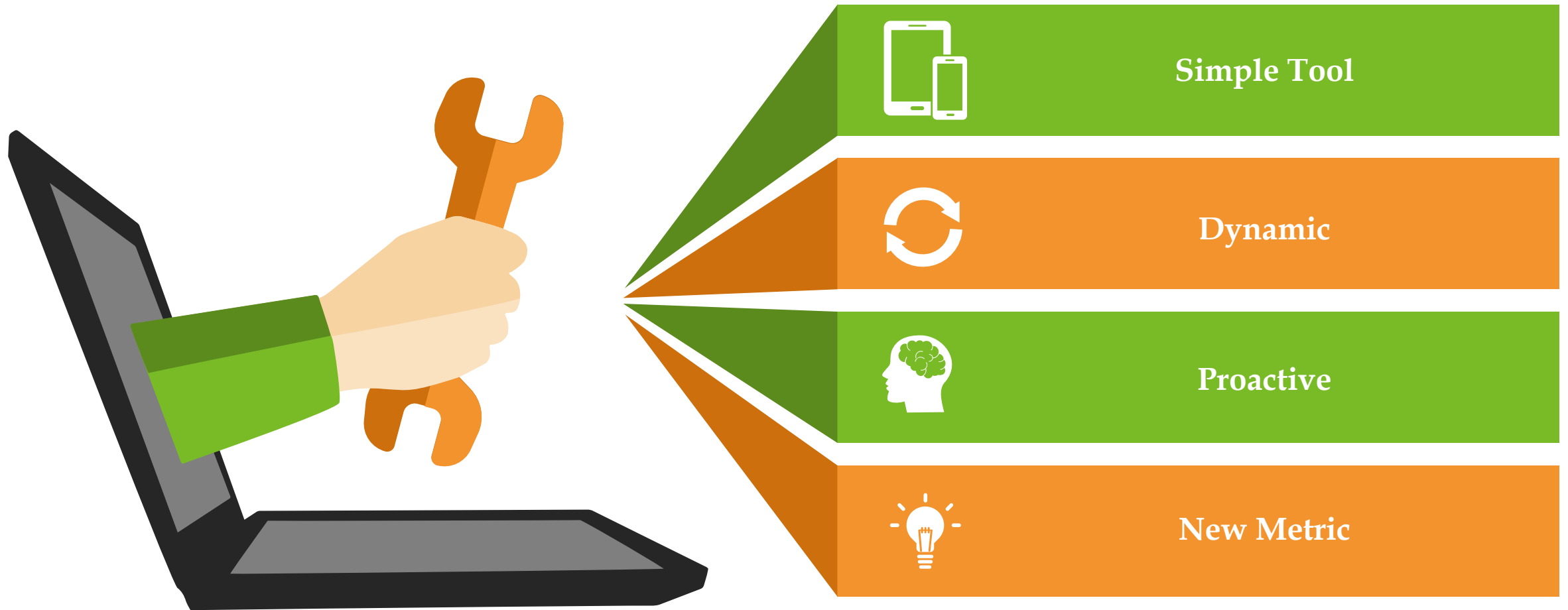




# Research Gap



# Goal





# Last Planner System

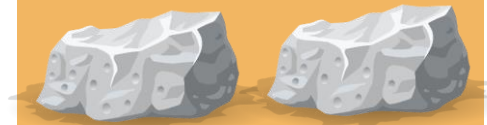
## Master Scheduling



Planners identify project milestones and major activities and perform push scheduling using the critical path method (CPM) to estimate the total project's duration (Hanzeh et al. 2008)

**SHOULD**

## Phase Scheduling



Planner break down phases developed in the master schedule into activities, identify gross constraints, and perform reverse phase scheduling (Hamzeh 2009)

**CAN**

## Lookahead Planning



Planners break down tasks from the phase schedule, design and detail their execution, and remove constraints to make tasks ready (Junnonen and Seppänen 2004)

**WILL**

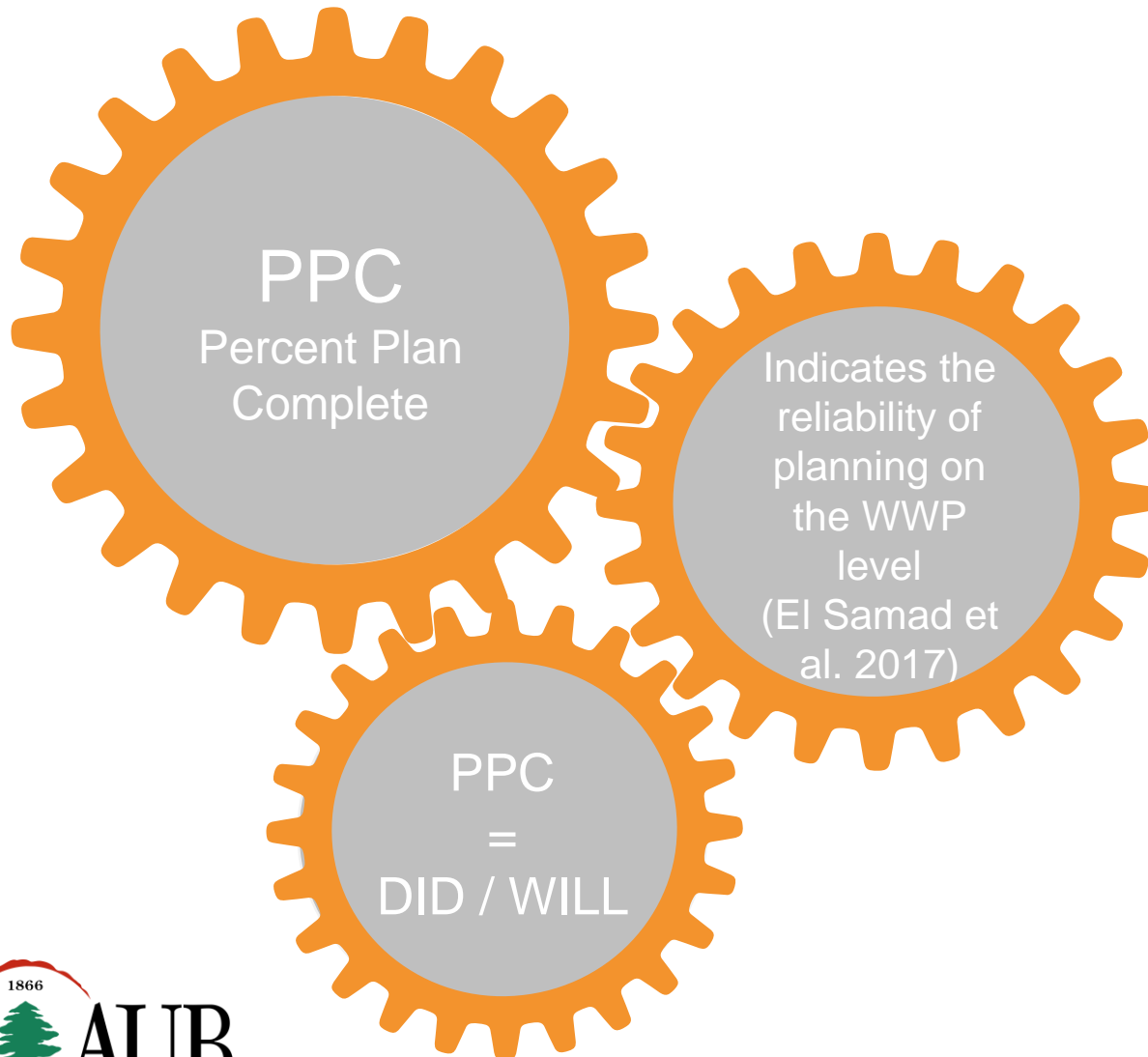
## Weekly Work Plan (WWP)



Planners should include sound assignments that are made ready by removing any constraints that prevent them from becoming ready for execution. (Ballard 2000)

**DID**

# LPS Metrics Used







# Control in LPS & Linear Scheduling

## SHOULD & CAN

SHOULD and CAN rather than just  
SHOULD and DID  
(Howell and Ballard 1996)

## Production Unit & Workflow

Ensure better workers assignments  
& ensure the best work sequence  
(Ballard 2000)

## Early Constraints Identification and Removal

To facilitate work plans' reliability  
(Hamzeh 2009)

## Metrics

For continuous improvement and  
learning from failures

## Monitor

Actual Progress

## Forecast

Future Progress

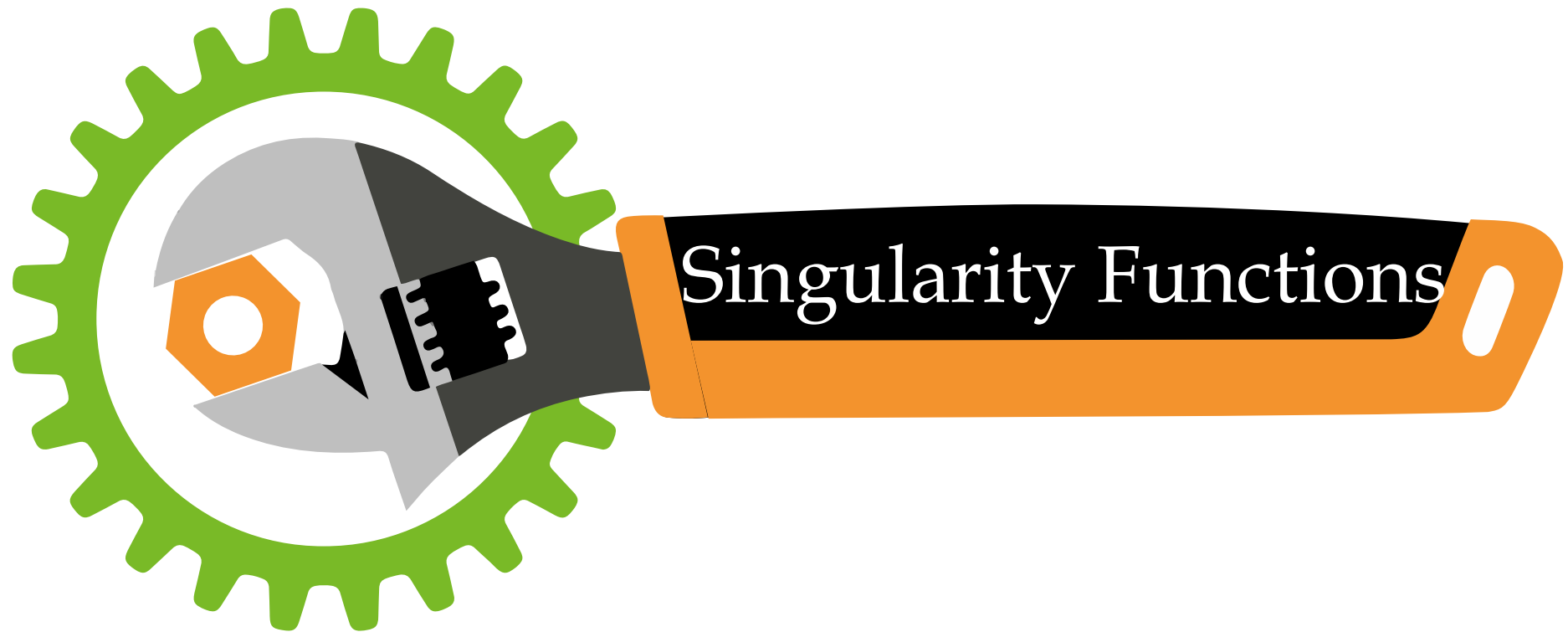
## Alert

Cascading Delays and Clashes  
(Seppänen 2013)

## Buffer

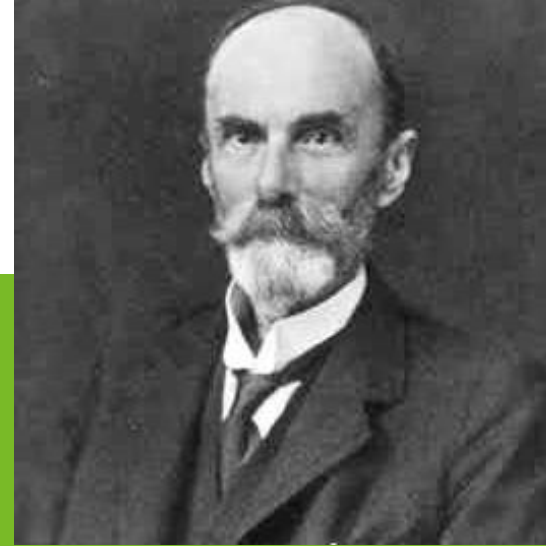
Time - Space - Plan (Frandsen 2015)





# Singularity

## Functions



Macaulay (1919)



Föppl (1927)



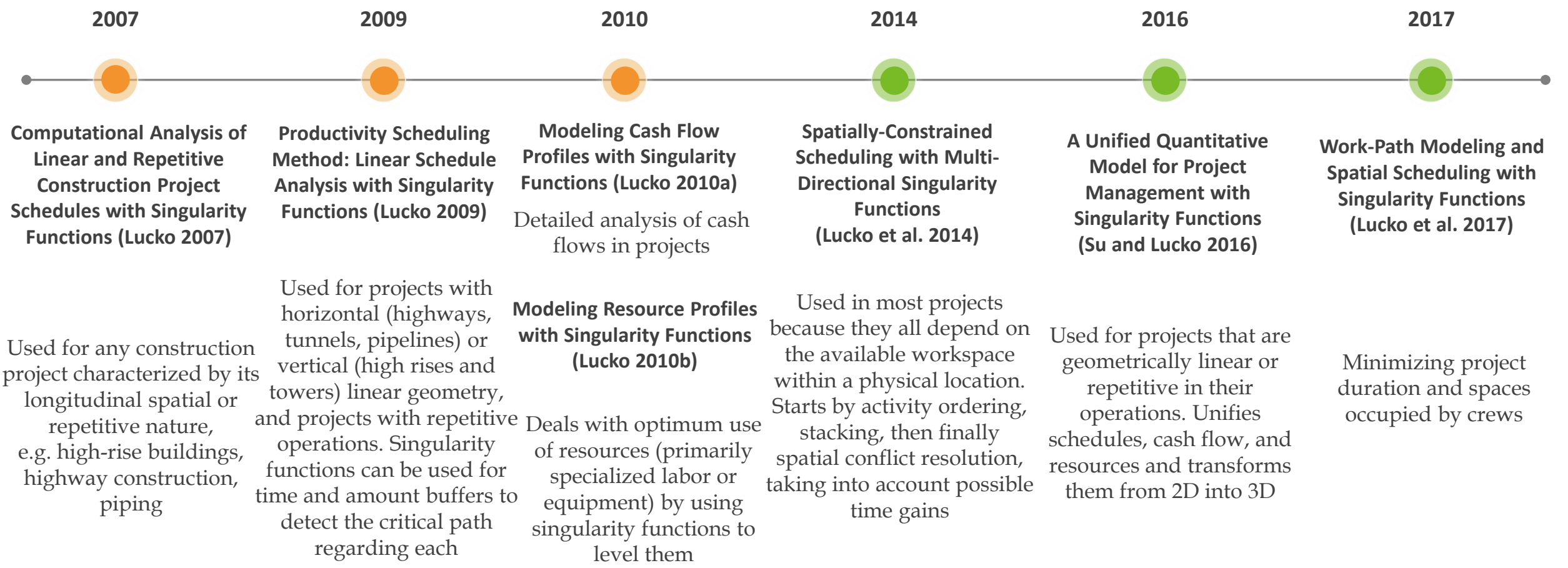
S = strength  
 x = variable under consideration  
 a = activation point  
 n = behavior shape  
 If n = 0 → step

If n = 1 → slope



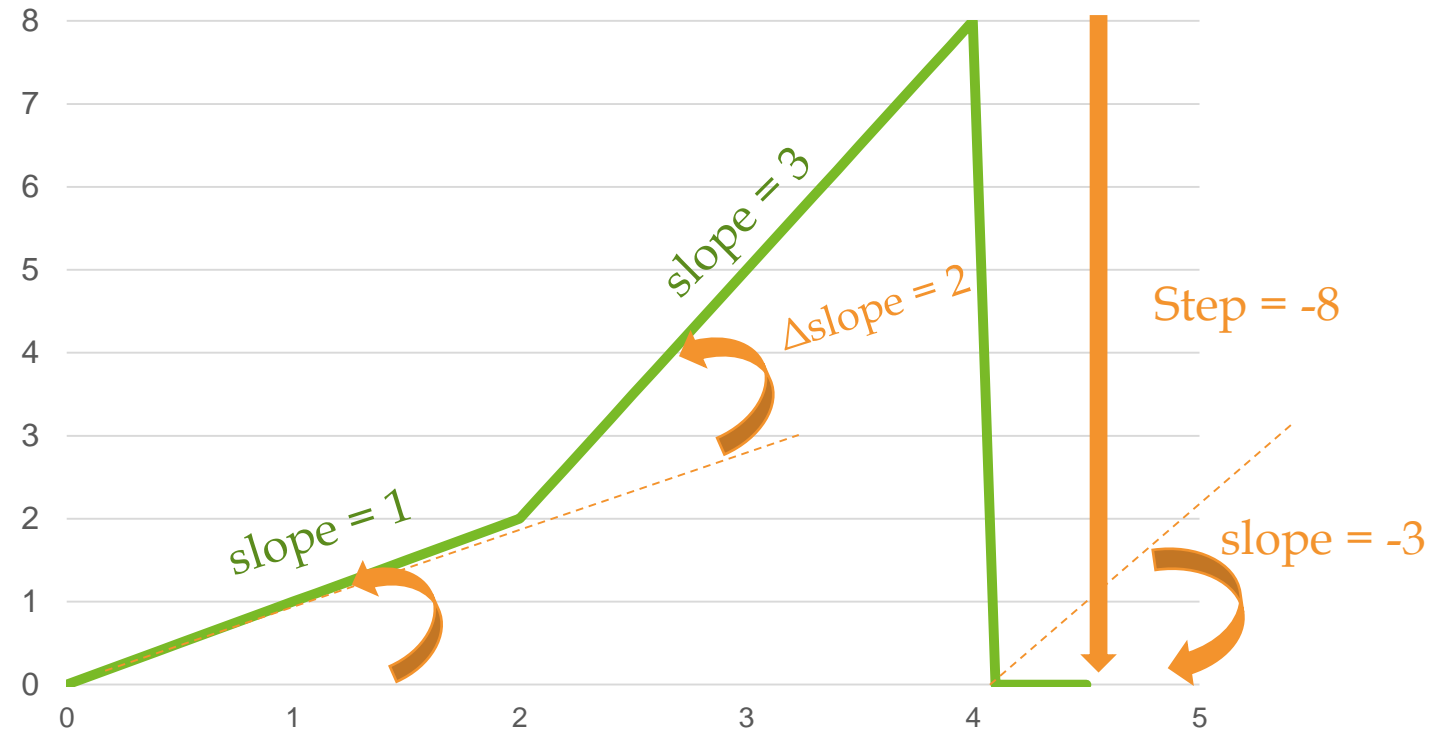
$$S < x - a >^n = \begin{cases} 0 & \text{for } x < a \\ (x - a)^n & \text{for } x \geq a \end{cases}$$

# Singularity Functions in Construction Management



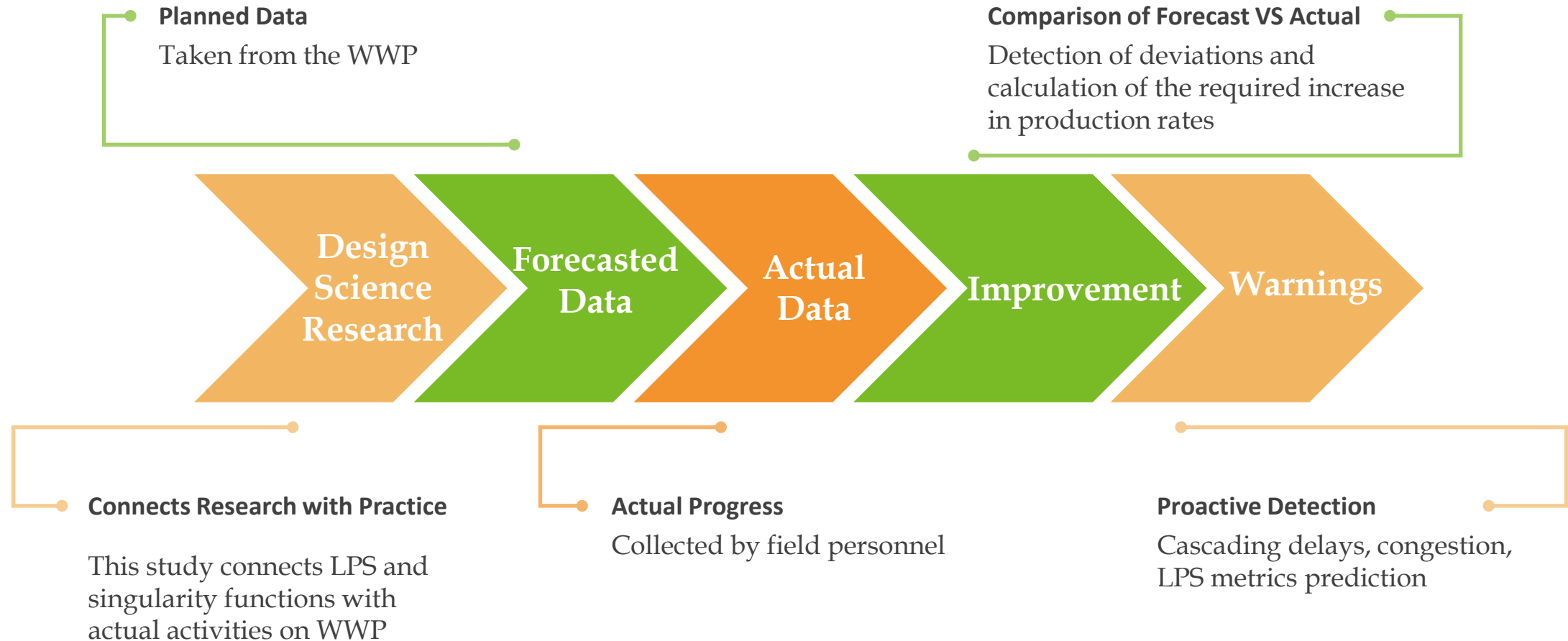
# Singularity Functions Example

$$\begin{aligned}
 W(t) = & \\
 & + 1 \langle t - 0 \rangle^1 \\
 & + 2 \langle t - 2 \rangle^1 \\
 & - 8 \langle t - 4 \rangle^0 \\
 & - 3 \langle t - 4 \rangle^1
 \end{aligned}$$

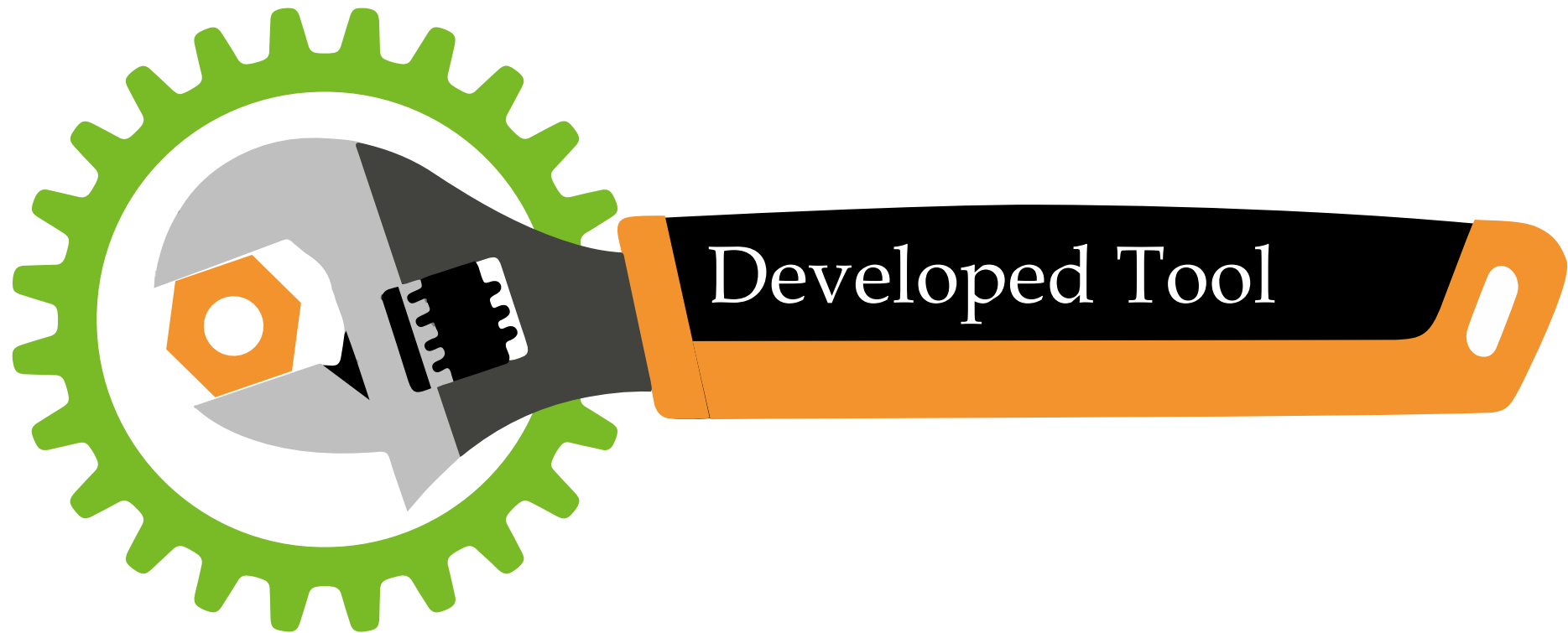




# Methodology







# Overview

## Item



**Forecast Activity Data**

**Actual Activity Data**

**Improvement of Activity**

**Resources Data**

## Input



Start Time  
End Time  
Work to be done

Actual Start Time  
End Time Before Improvement  
Work Done So Far

Required End Time

Number of Workers  
Maximum Production Rate  
Working Area  
Congestion Limit

## Output



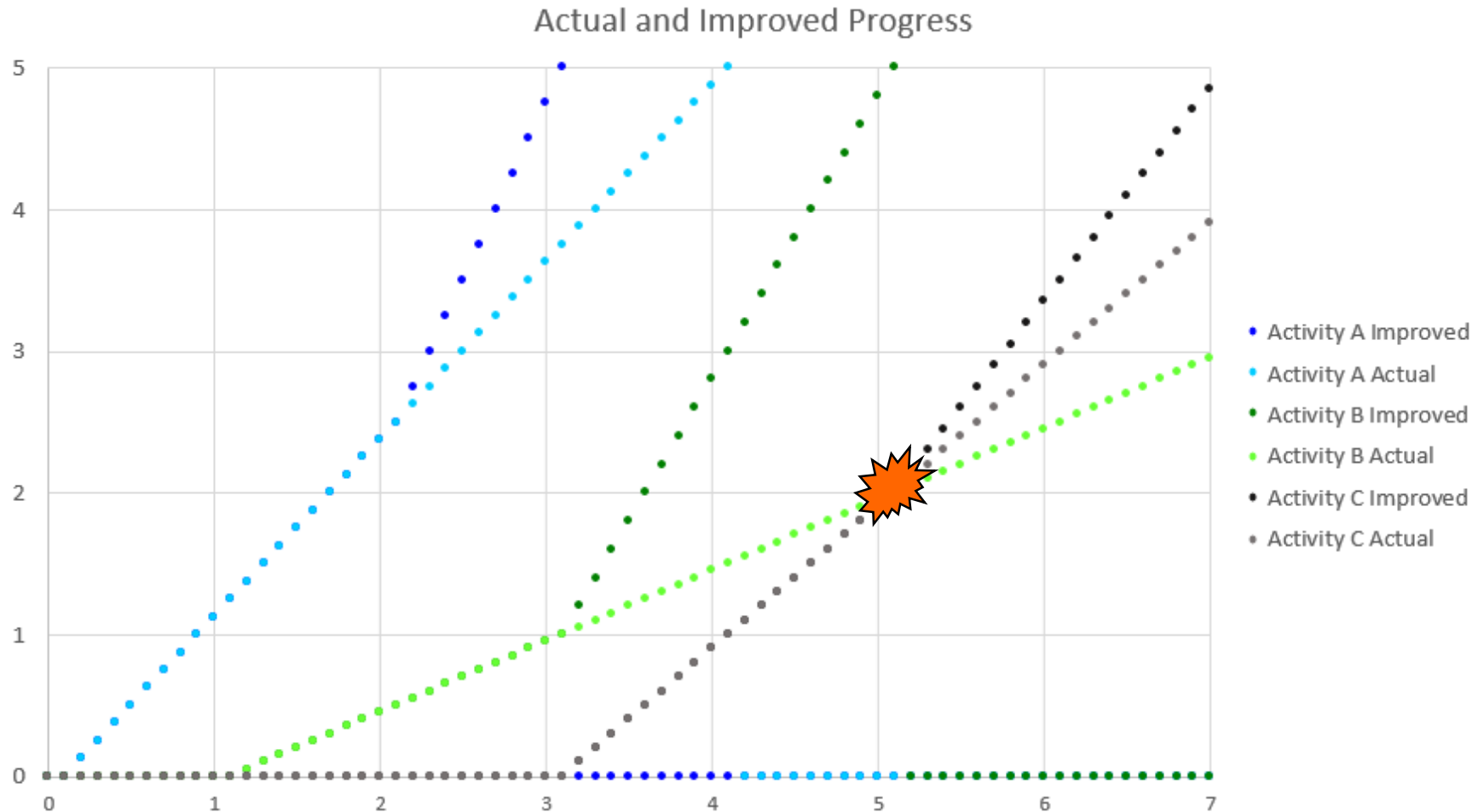
Planned Production Rate

Actual Production Rate  
PRI  
Warning of Cascading Delays  
Prediction of Metrics

Required Improved Production Rate

Modified Maximum Production Rate  
Warning of Resource Allocation if needed  
Warning of Congestion

# Visual Monitoring





# Proposed Metric

## Percent Improvement Complete PIC

$$\text{PIC} = \frac{\text{No. of Activities That Needed Improvement and Were Completed}}{\text{No. of All Activities That Needed Improvement}}$$

$$\text{PIC} = \frac{\text{Should \& Did Improve}}{\text{Should Improve}}$$

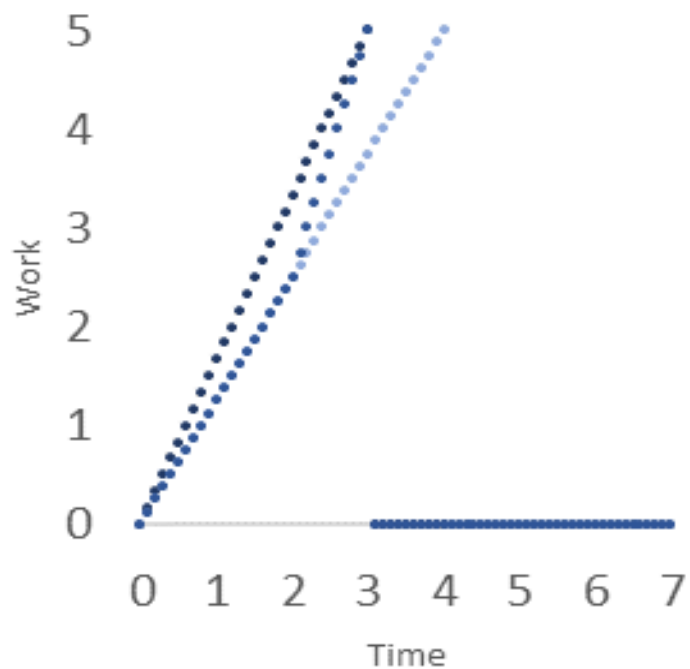
### Purpose

Shows the reliability, ability, and commitment of the team in finishing the tasks that needed improvement

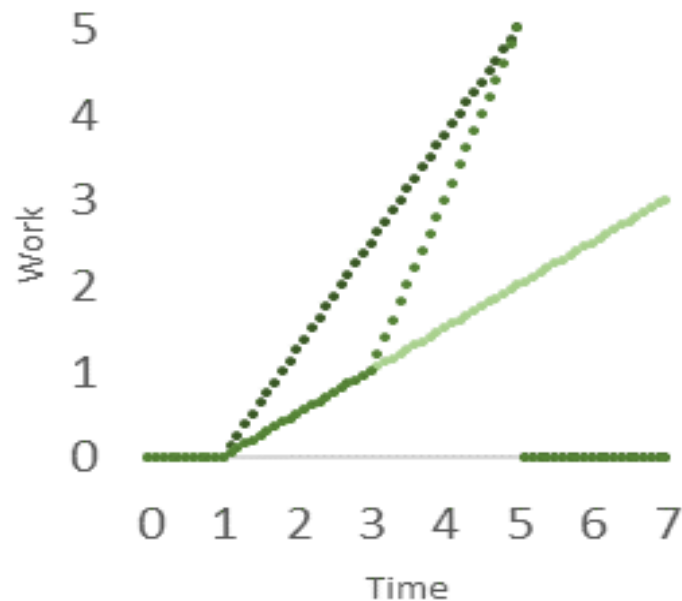


# Example

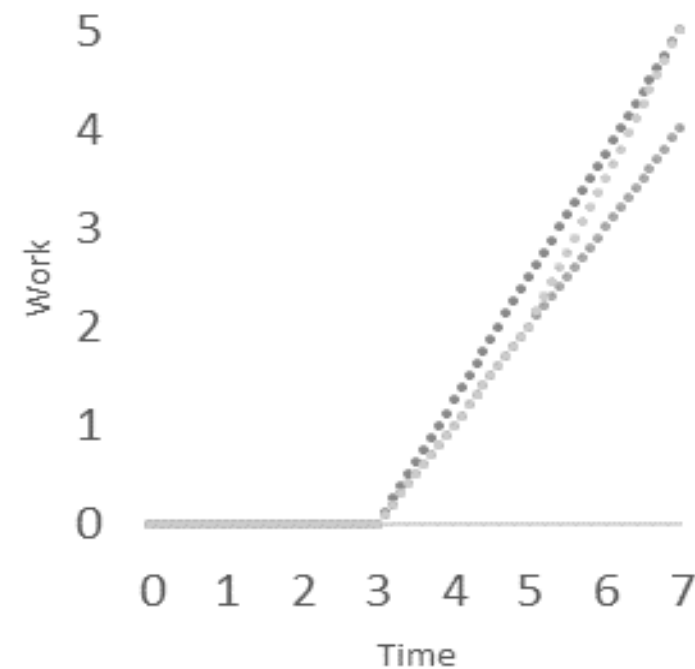
• Activity A Wf • Activity A Wn • Activity A Wi



• Activity B Wf • Activity B Wn • Activity B Wi



• Activity C Wf • Activity C Wn • Activity C Wi



# of Tasks that need Improvement

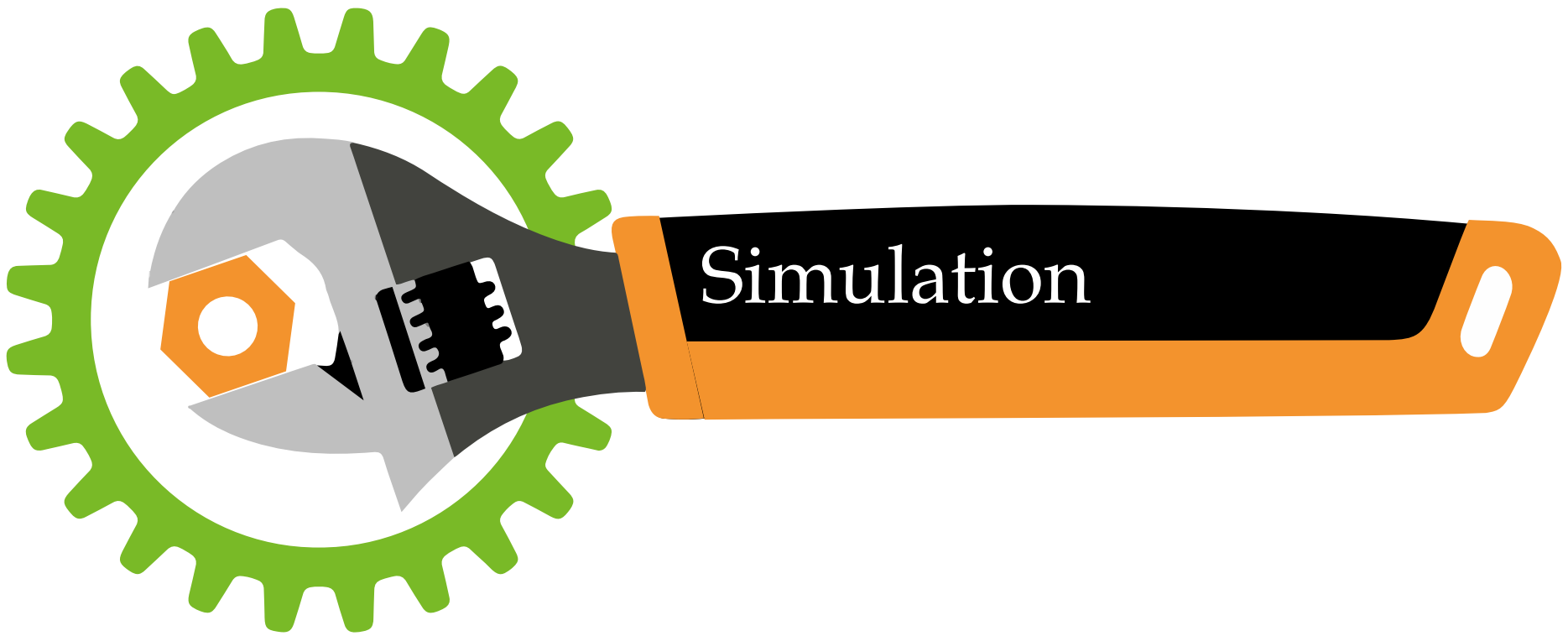
3

# of Tasks that need Improvement +  
were completed

2

Percent Improvement Complete (PIC)

67%



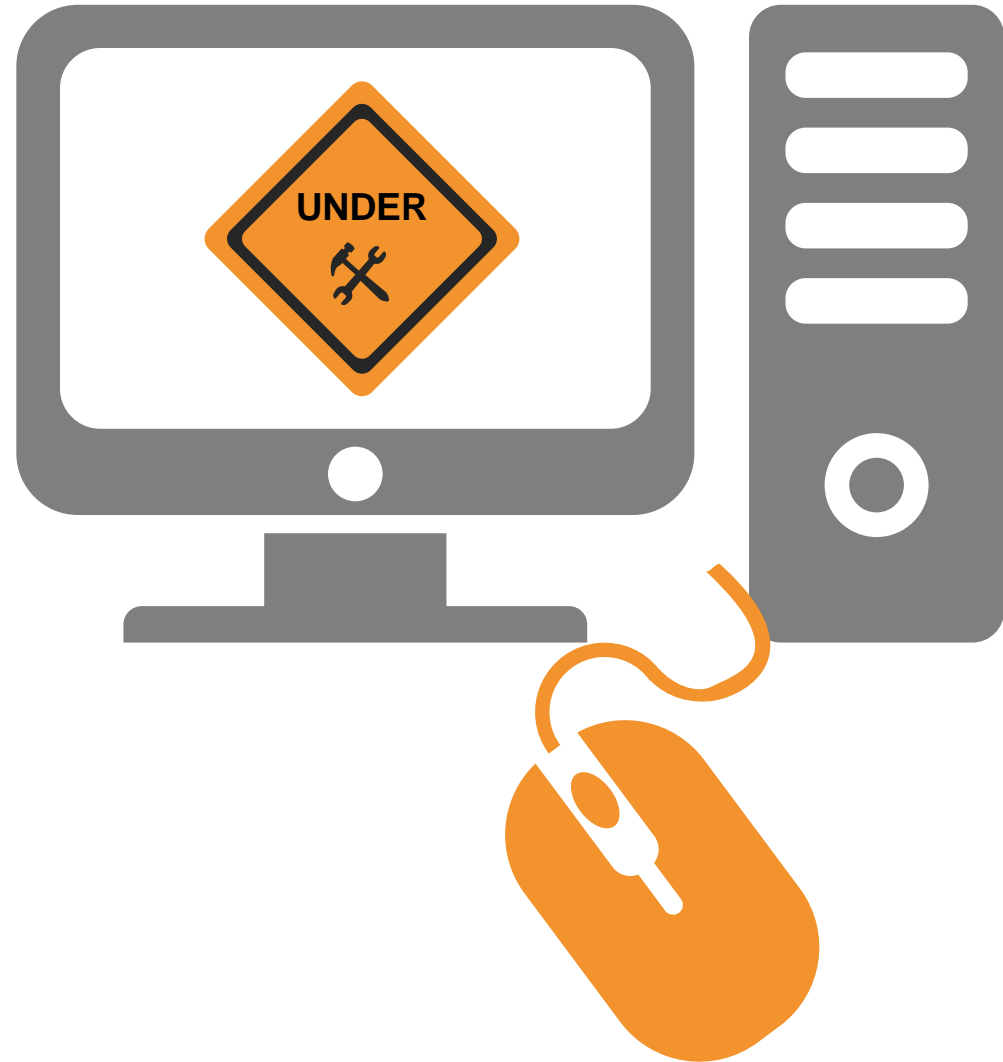
# THE NEED FOR SIMULATION



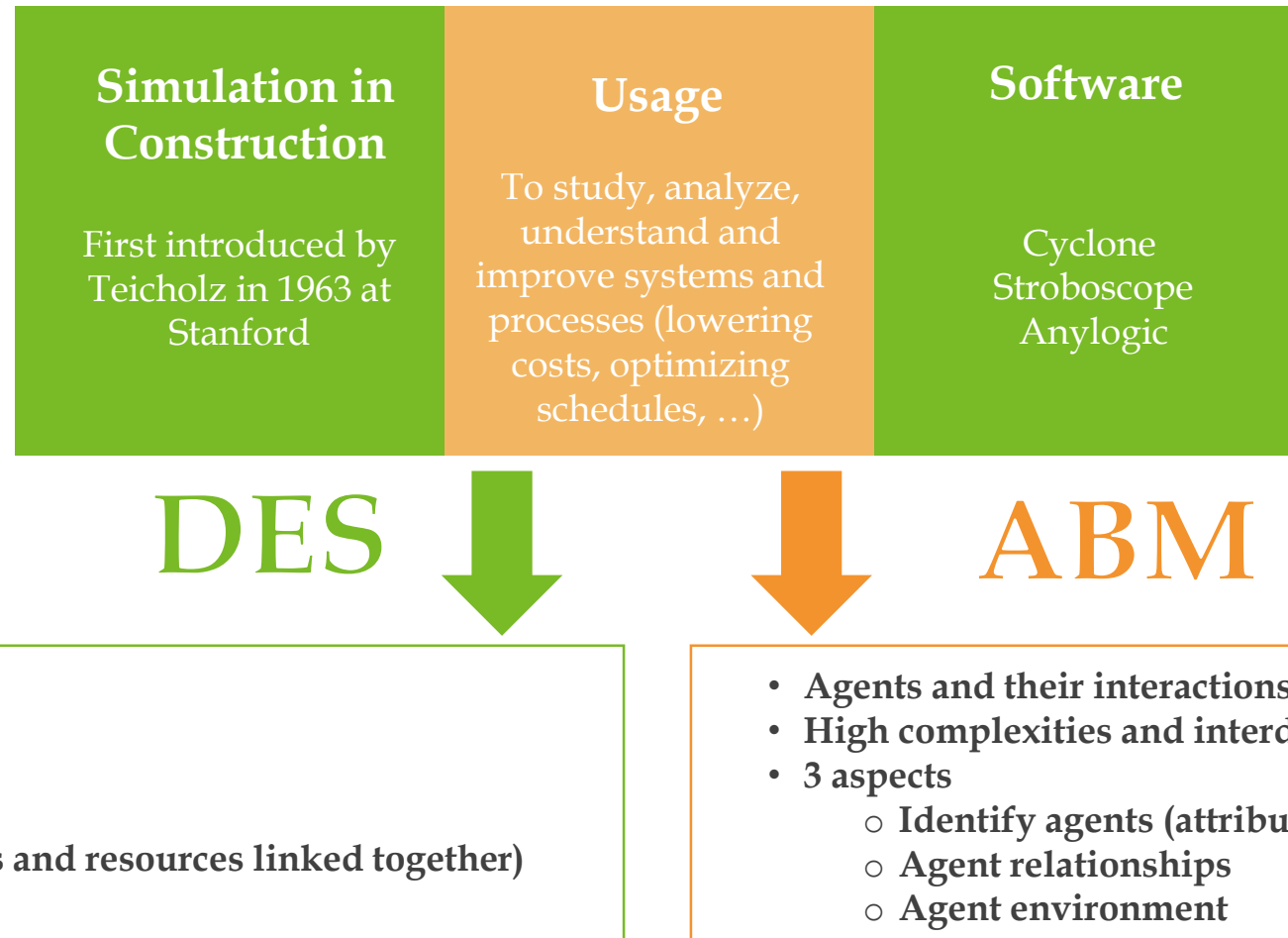
Lack of an ABM & DES  
Simulation Model



Metrics Not Used In Production  
Rate Calculation



# Simulation





# Overview

Purpose: Achieve more accurate values of the Improved Production Rate (IPR) obtained from singularity functions

Inputs from  
EXCEL

- Congestion
- Time remaining for improvement
- Minimum, mode and maximum values for PIC, PRI, PPC and CLR

Input  
Analysis

- DES
- ABM

Output

- Modified Time left for improvement and converted into a graphical production rate form in EXCEL
- Find the “most likely” production rate

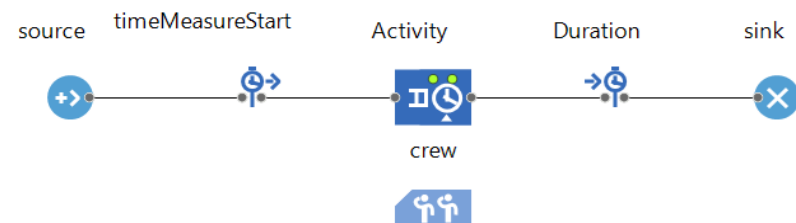


Figure 1 – Discrete-Event Process

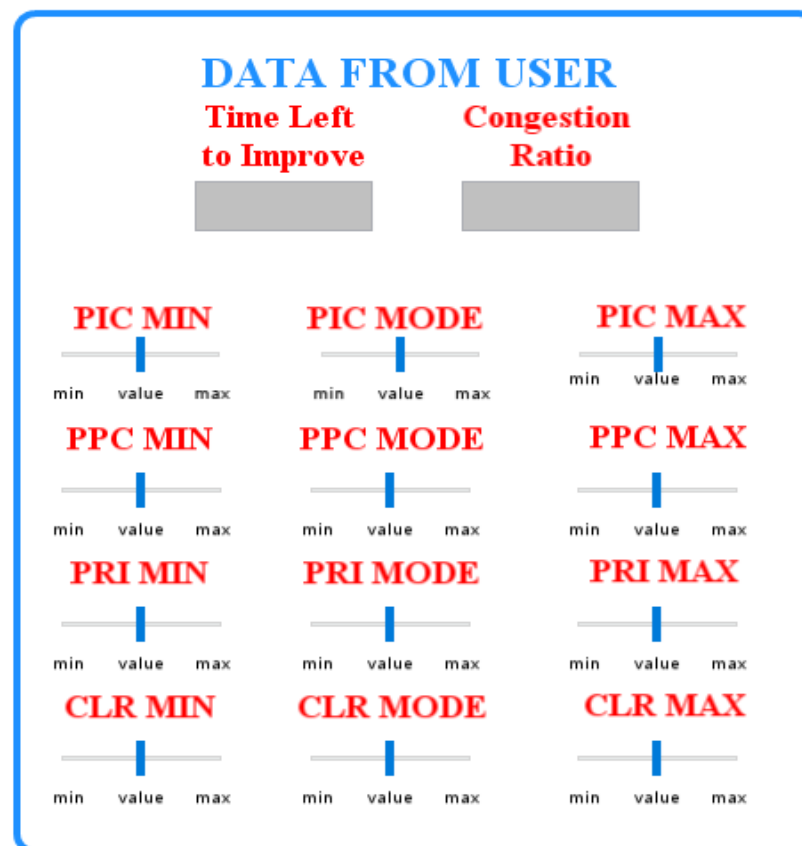


Figure 2 - User Dashboard

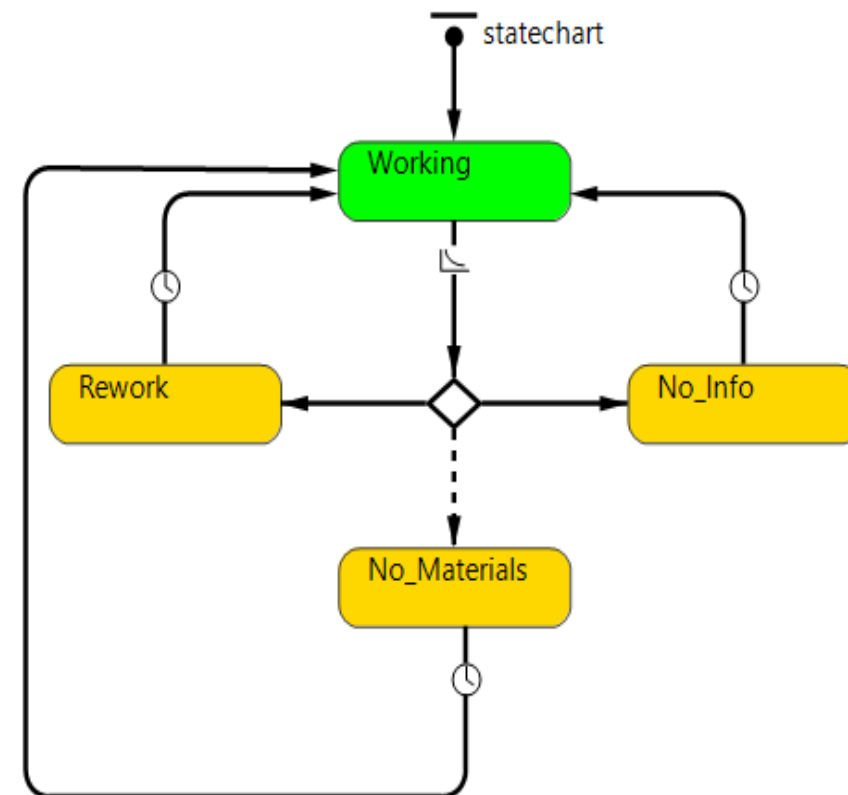


Figure 3 - Crew Statechart

Run  
the  
model



Calculate modified duration  
1000 times



Convert each modified  
duration into a production rate



The “most likely” IPR is  
automatically calculated



Realistic approximation of the rate that the crew will most probably work at to execute the work required, by taking into account congestion, idleness, and the LPS metrics

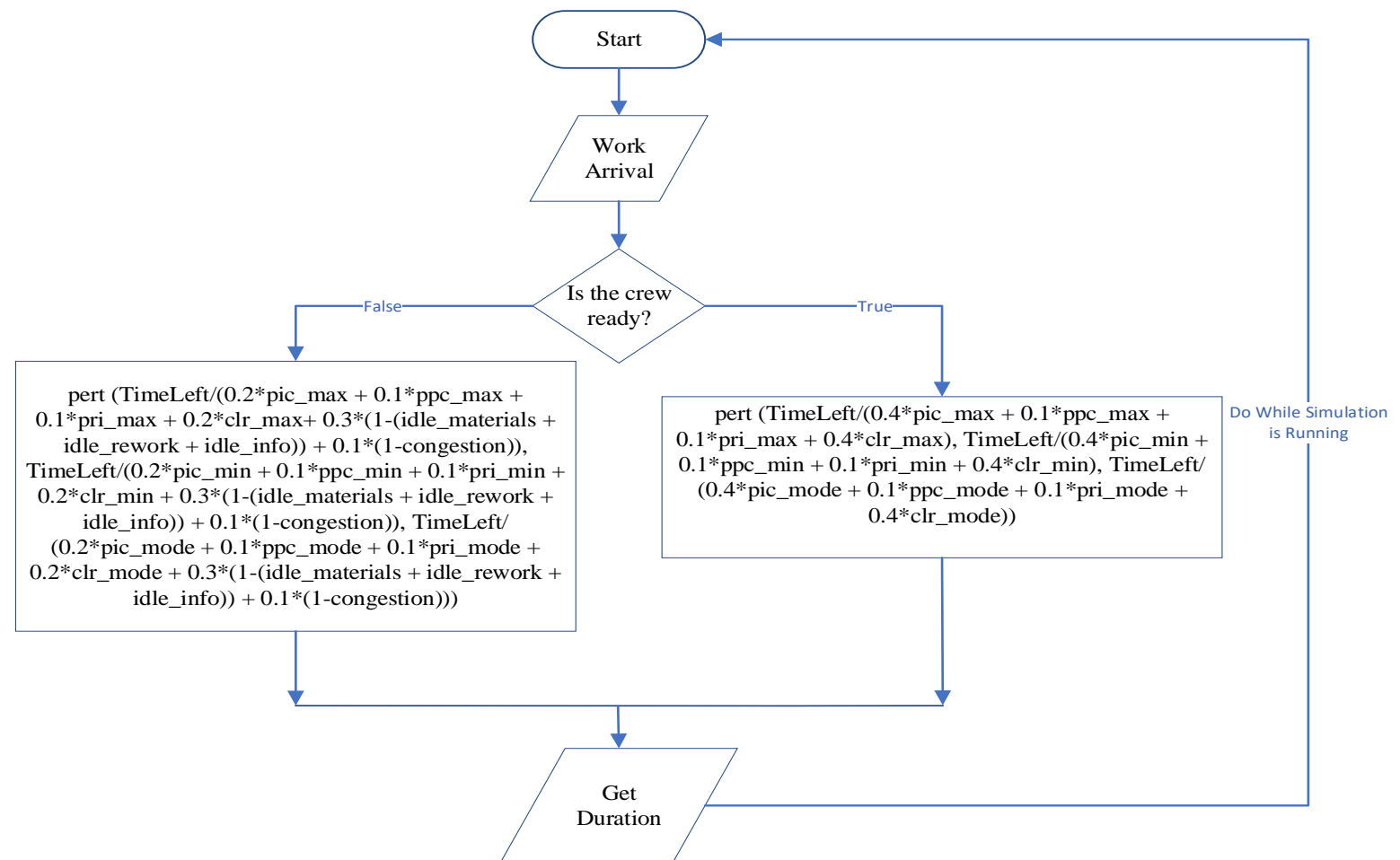
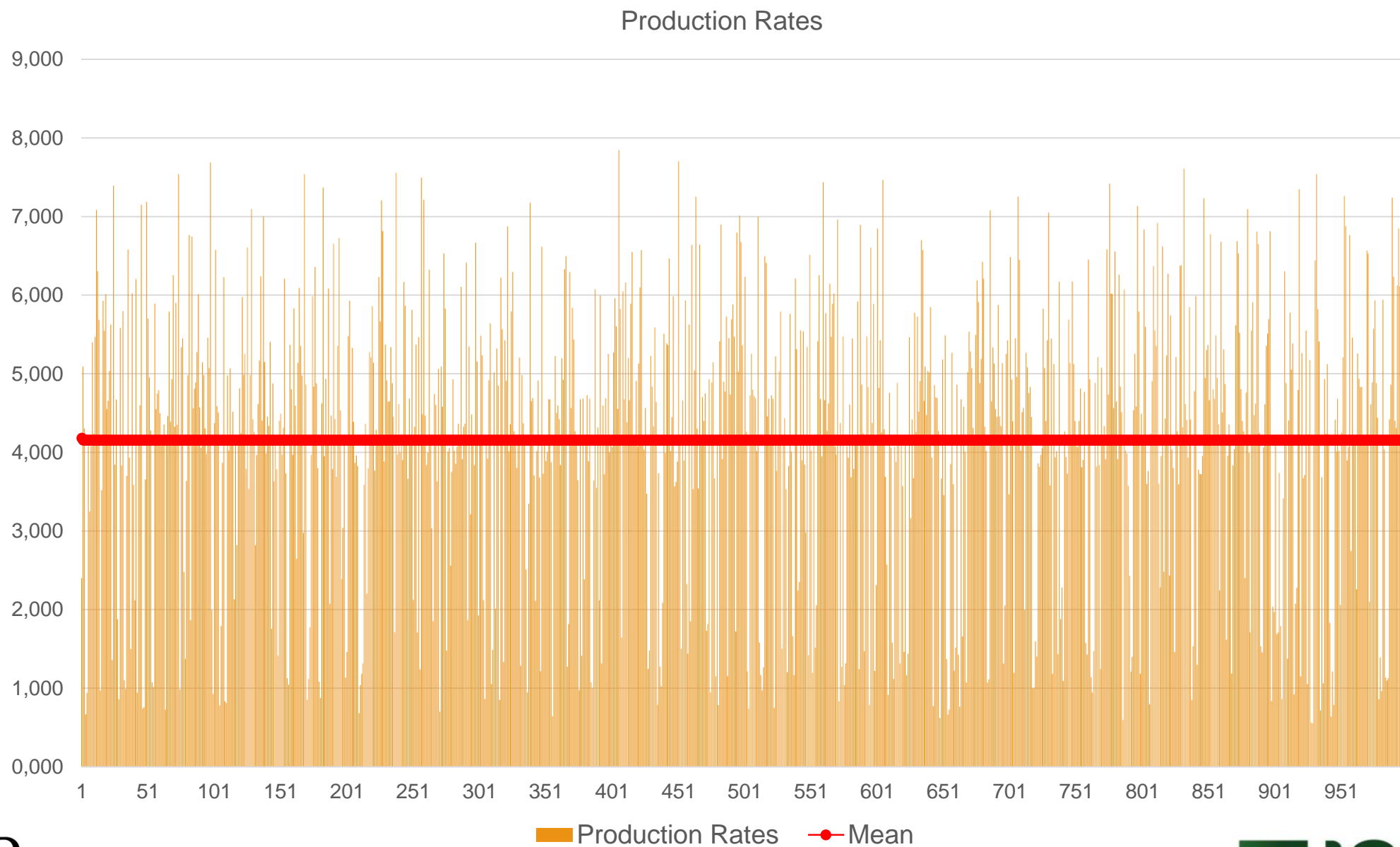


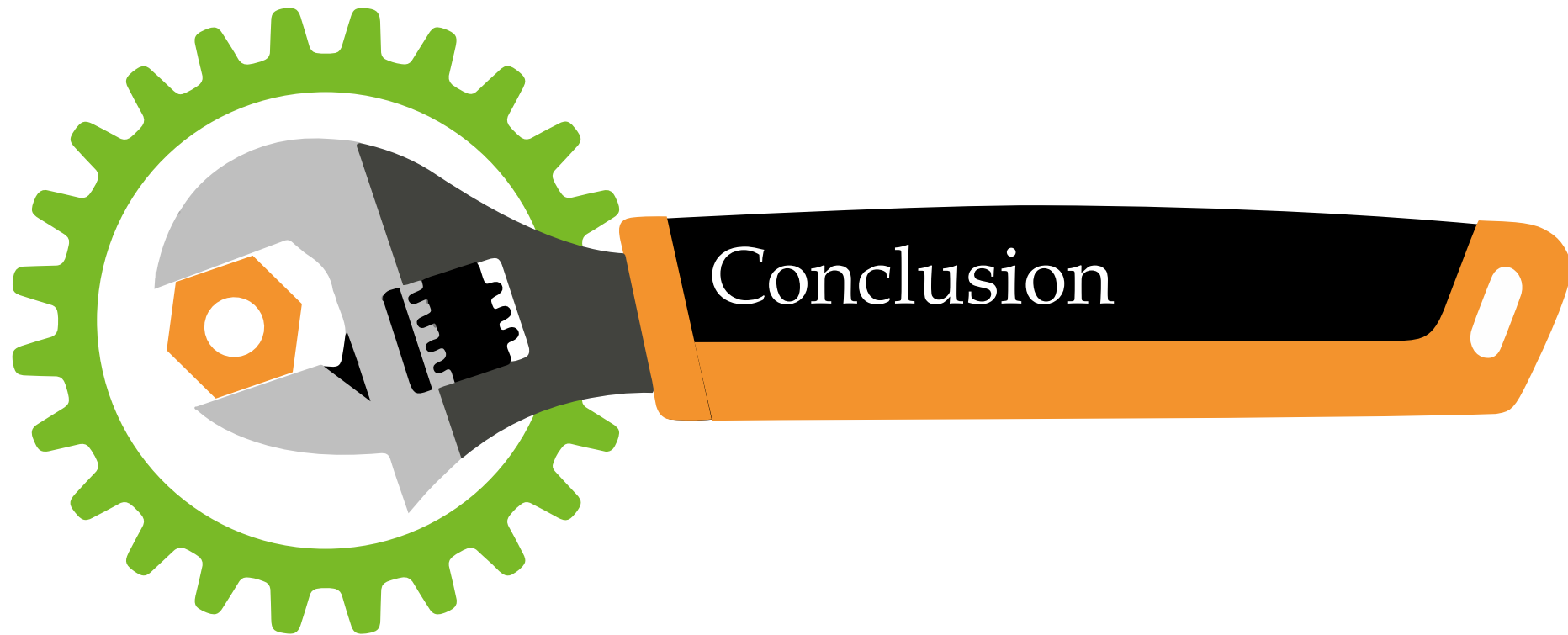
Figure 4 - Anylogic Flowchart

# Simulation Runs

Time left for improvement = 1 day

Experiment	Min. Metrics	Mode Metrics	Max. Metrics	Congestion	Mean Duration	Most Likely IPR
Good performance	0.7	0.9	1	0.2	1.65	6.84
Average performance	0.4	0.6	0.8	0.5	3.38	4.18
Bad performance	0.1	0.4	0.5	0.9	7.41	2.54





# Conclusion & Future Research

- A tool to monitor project performance at the level of the WWP of LPS
- Singularity functions to monitor and forecast activity progress
- Several metrics from the LPS are used
- A new metric (PIC) is suggested for the reliability to implement required improvements during execution.
  - Shows the reliability of the promises made during the week of execution
  - Use along with the maximum production rates that are modified by PRI to ensure that the required improvements are rational and within the crew's capacity.



- Additional metrics can be developed showing the volume of improvement
- This method should be tested on an actual project as a case study and refinements could be made.
- Improvements in the production rates should be linked to Takt Time for all the activities.



# Thank You